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## CSCI 151

## Exam 2

## December 17, 2021

This is a closed-book, closed-notes, closed-Internet exam.

The exam has 6 numbered questions; each is worth 16 points. You get 4 points for free, for a total of 100 points.

The last page of the exam is blank; you can use this for additional space for any of the exam questions.

After you have finished the exam please indicate whether you followed the Honor Code on the exam.

। $\square$ did $\square$ did not adhere to the Honor Code while taking this exam.

1. Here is a picture of a binary tree. Give pre-order, in-order, and post-order traversals of this tree.


Pre-order:

In-order:

Post-order
2. We have discussed three $O\left(n^{*} \log (n)\right)$ sorting algorithms this semester: MergeSort, QuickSort, and HeapSort. Choose one of them - any one you wish..
A. Describe in one or two sentences how this algorithm works.
B. What is one feature of this algorithm that would either incline you to use it or not to use it?
3. Here is an AVL tree. Draw the AVL tree that results from inserting $\mathbf{2 5}$ into this tree.

4. Here is a list of values and their hash codes:

| value | 4 | 2 | 18 | 19 | 11 | 7 | 9 | 0 | 15 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| hashcode | 4 | 2 | 0 | 1 | 2 | 7 | 0 | 0 | 6 |

Add these values from left to right (first 4, then 2 , then 18 ...) to the following hash table. The small numbers are the table indices, so you don't have to count across to see where an index such as 6 occurs.

| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |  |  |

5. We have a linked list class based on the following structure:
class MyLinkedList \{
Node head, tail;
MyLinkedList( ) \{
head = new Node();
tail = new Node();
head.next = tail;
\}
\}
To save space I am not going to write the Node class. Nodes have an integer value data and a link next. There are two Node constructors; one takes an integer argument and builds a Node with that value; the other takes no argument and builds an empty Node. You can directly access the fields of a Node: if $x$ and $y$ are Nodes you can say things like $x$. next $=y$; and $x$.data $=23$.
Here is a picture of a typical list. Note that head and tail are empty sentinel nodes guarding the front and rear of the list; the list is empty when head points to tail.


Give a method InsertInOrder(int d) for the MyLinkedList class that will insert a new element $d$ into the list so that, if the list is ordered from smallest to largest before this method is called, then d will be inserted at a location that preserves the order. For example, if we call InsertInOrder(25) with the list pictured, 25 will be placed between 20 and 30.
6. Here is a class for Binary Search Trees that holds integer values
public class BST \{
int value;
BST left, right;
int size; // the number nodes in the tree with this as root
\}
Below is a picture of a tree using this structure. Note that there is no EmptyTree class; empty trees are represented by null pointers. Write a method for this class int kth(int k)
that returns the kth largest value in the tree. For the tree pictured $k t h(0)$ is $4, k t h(1)$ is $10, k t h(2)$ is 20 and $k t h(4)$ is 50 . You can assume $k$ will be between 0 and the size of the tree; you don't have to test for that.


A cheesy way to do this is to put all of the values into a list, sort the list, and return the value at index $k$. Instead of that, I am looking for a recursive solution.

You can use this page for additional space for any question.

